

Quantum secure message authentication via blind-unforgeability

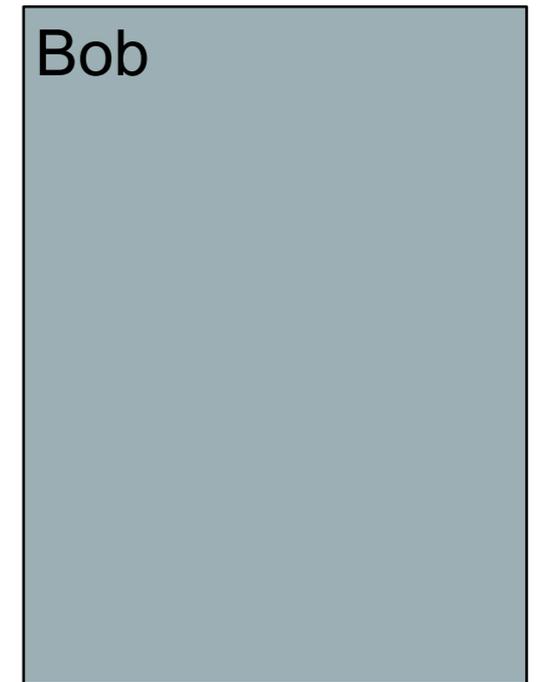
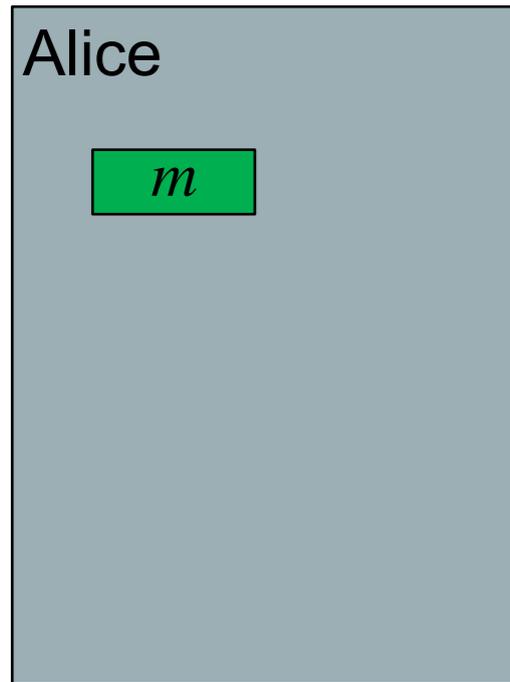
Christian Majenz

Joint work with Gorjan Alagic, Alexander Russell and Fang Song

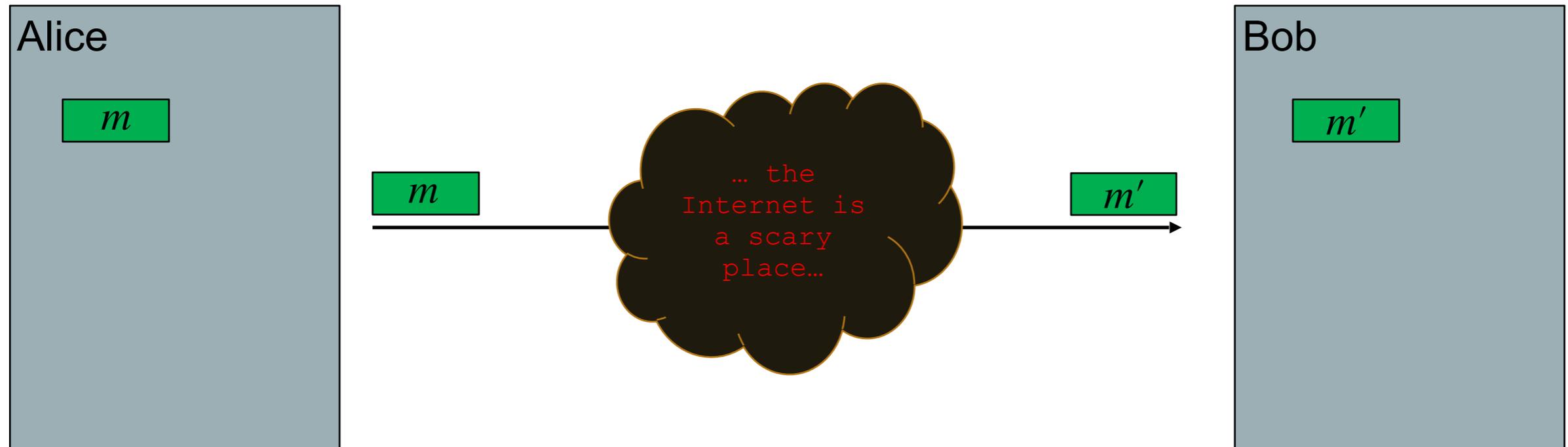
QCrypt 2018, Shanghai, China



Message authentication

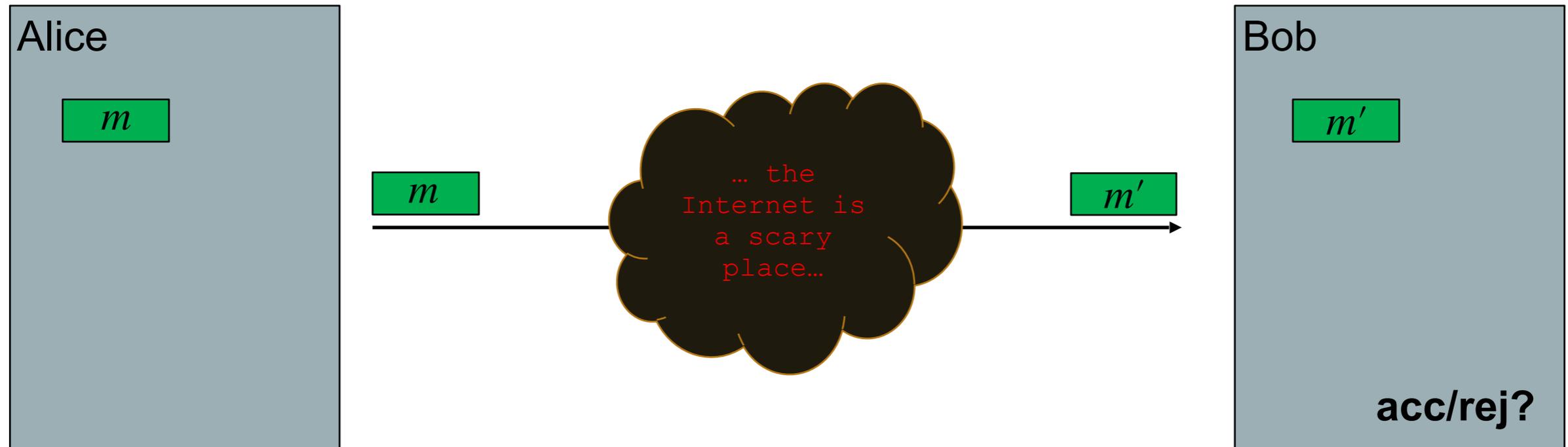


Message authentication



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Problem: how can Bob check if a message came from Alice and is unchanged?



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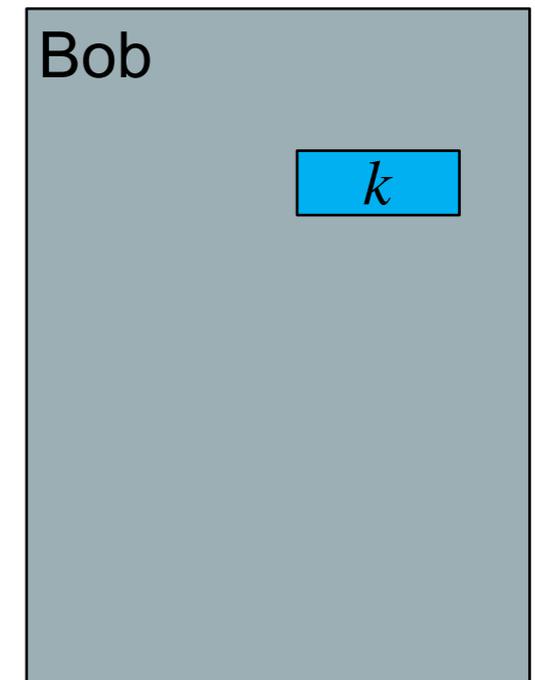
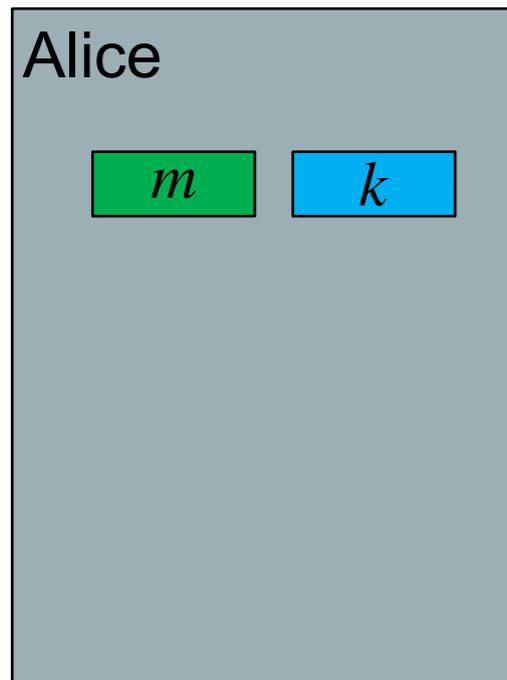
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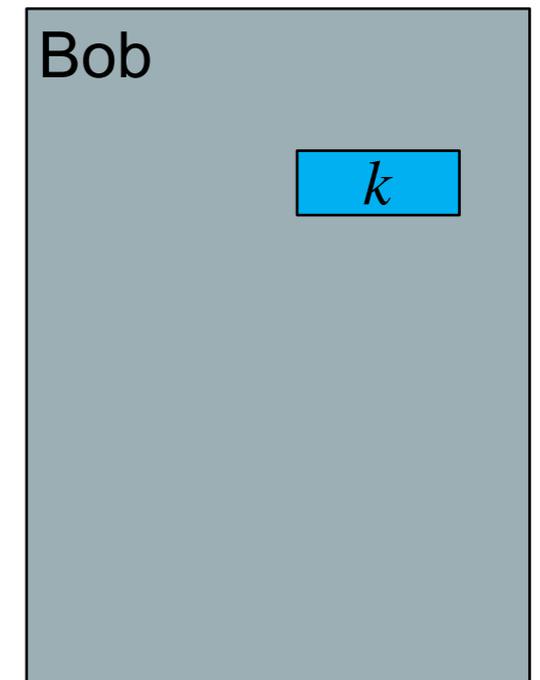
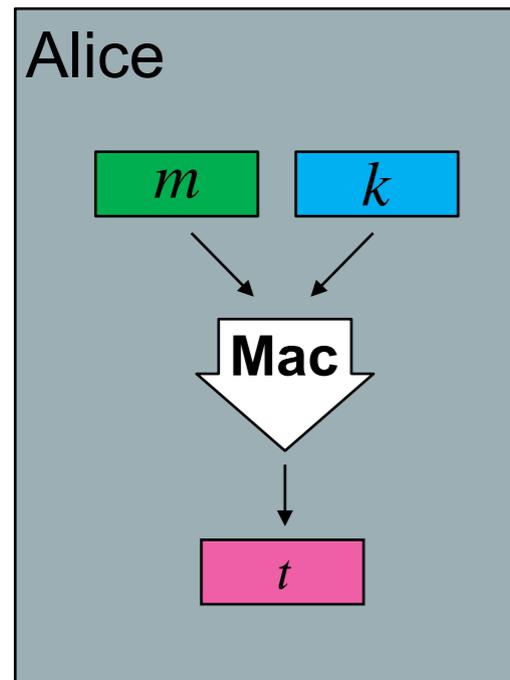
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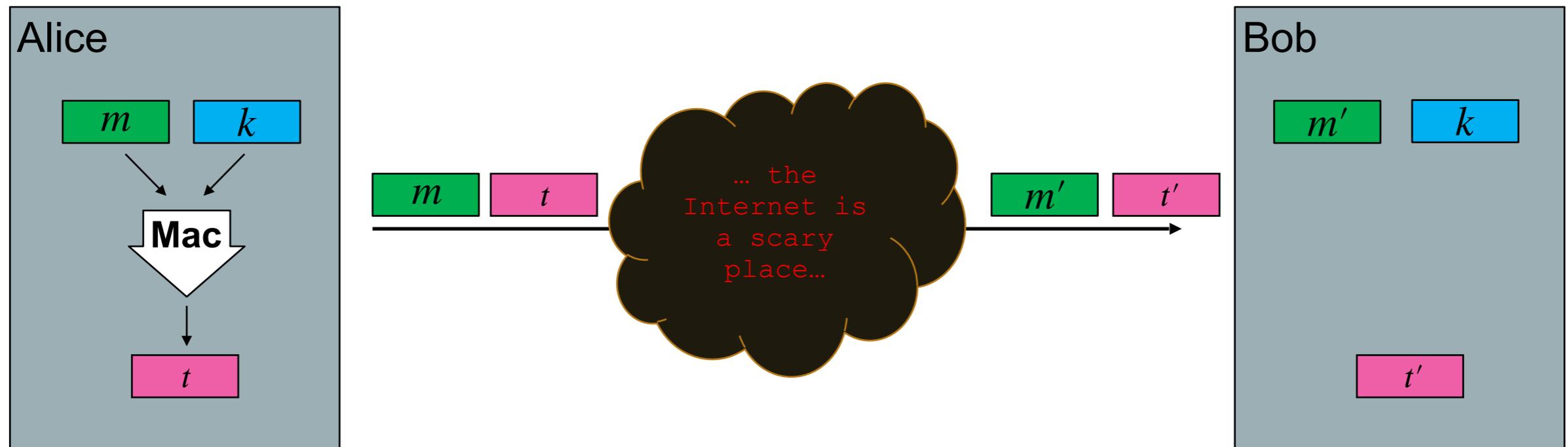
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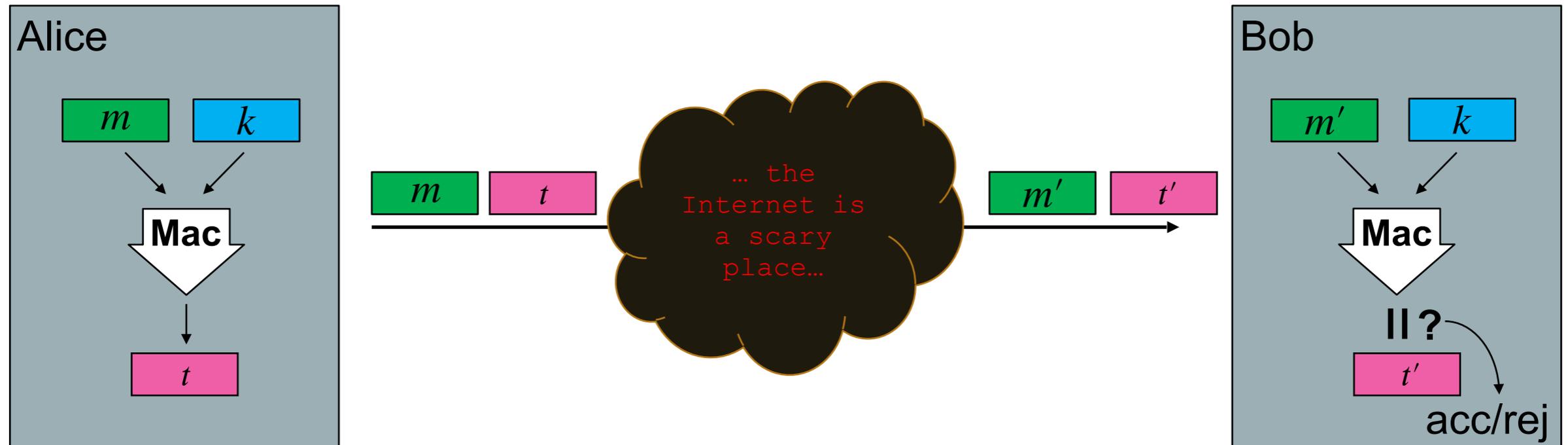
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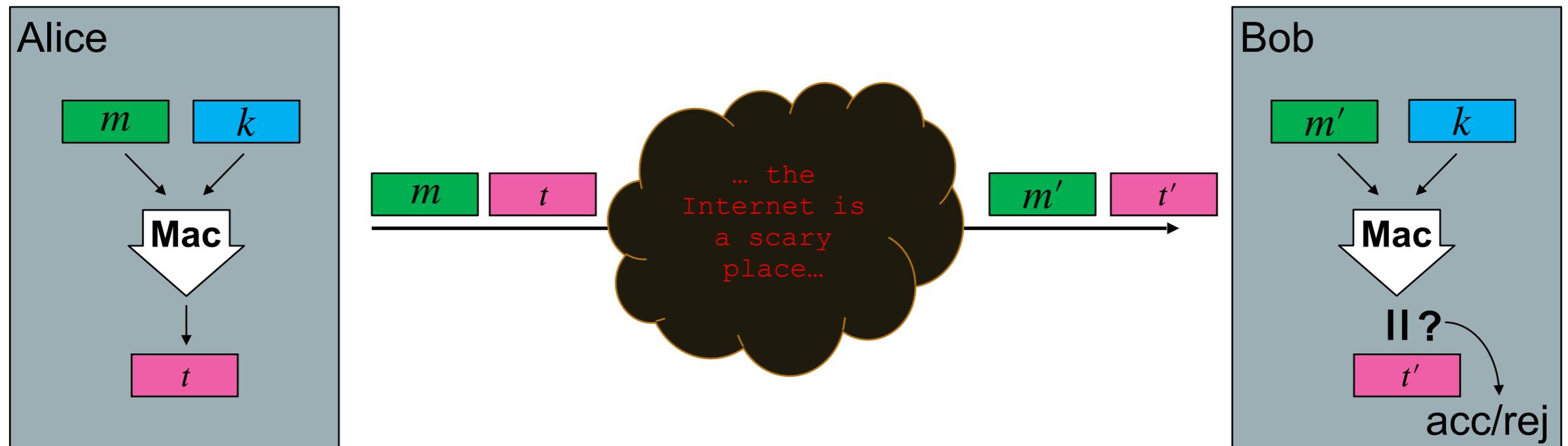
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Note: Bob is only checking *consistency with the function* .

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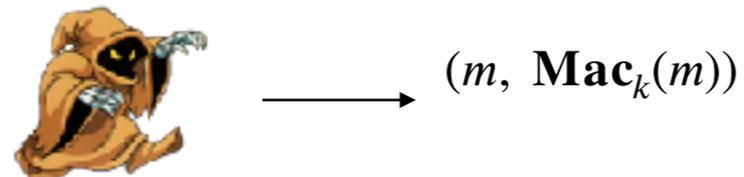
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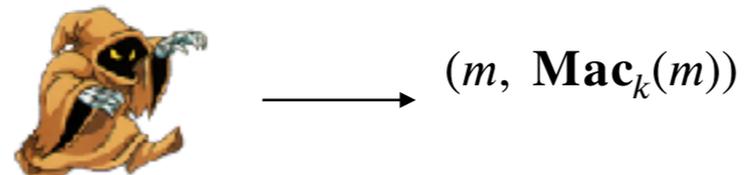


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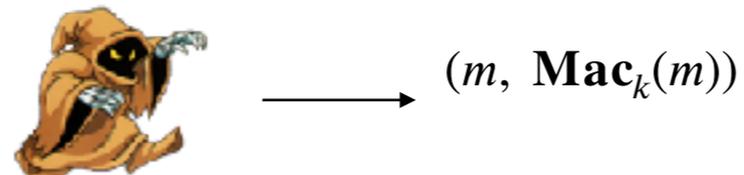


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Key property: *unpredictability* of Mac_k .

Classical security: Unforgeability

A message authentication code is secure, if no successful forger exists:

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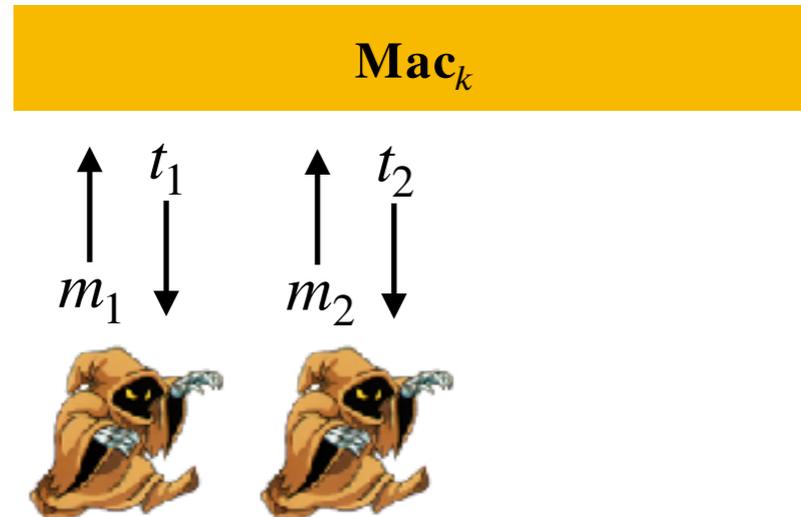
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m_1 t_1



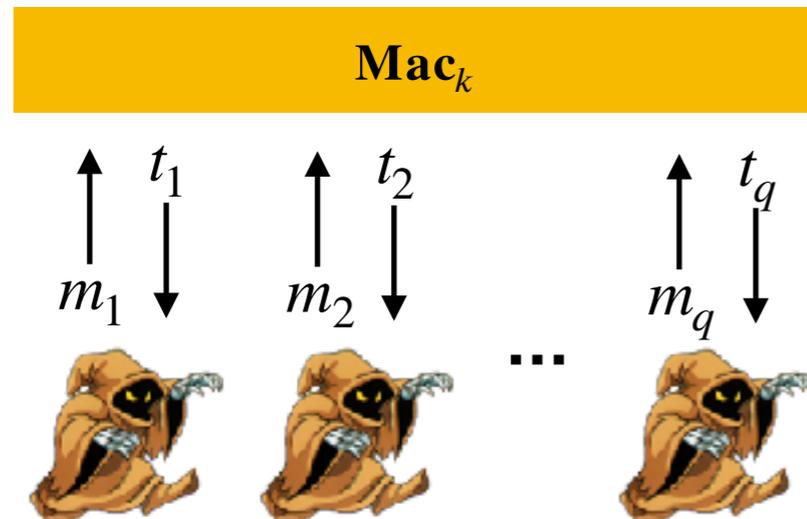
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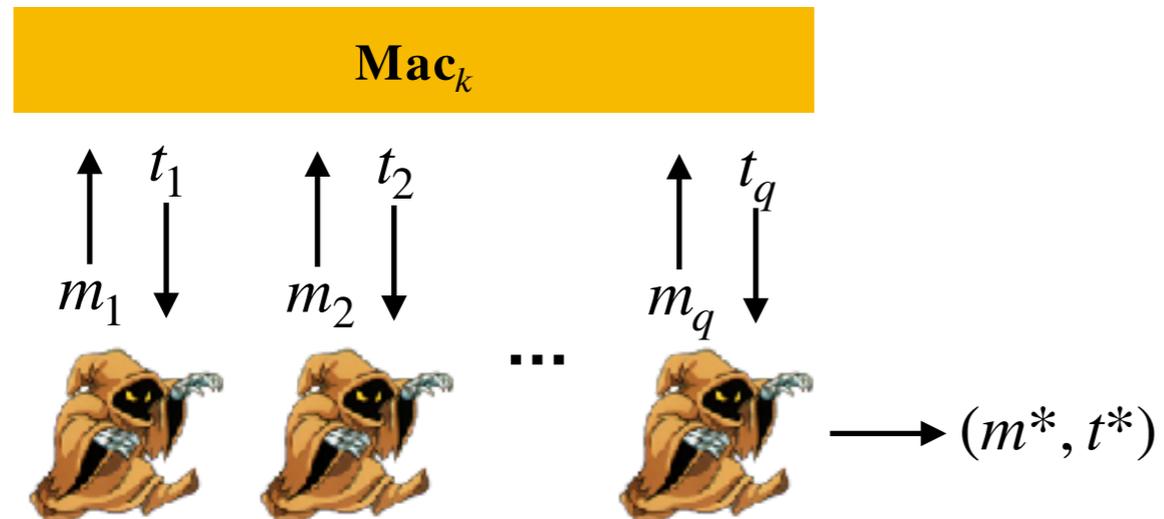
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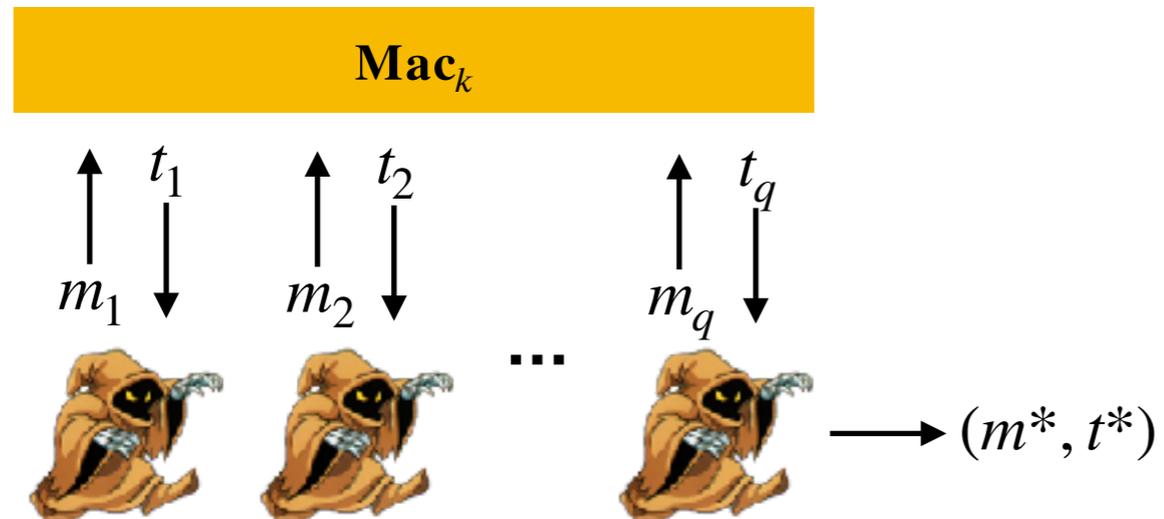
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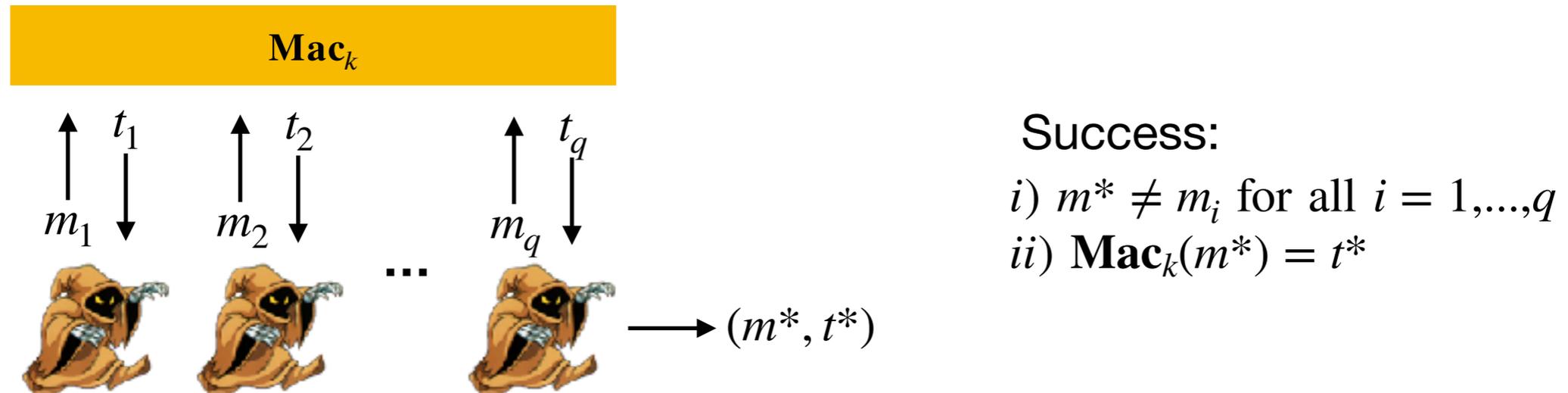


Success:

- i) $m^* \neq m_i$ for all $i = 1, \dots, q$
- ii) $\text{Mac}_k(m^*) = t^*$

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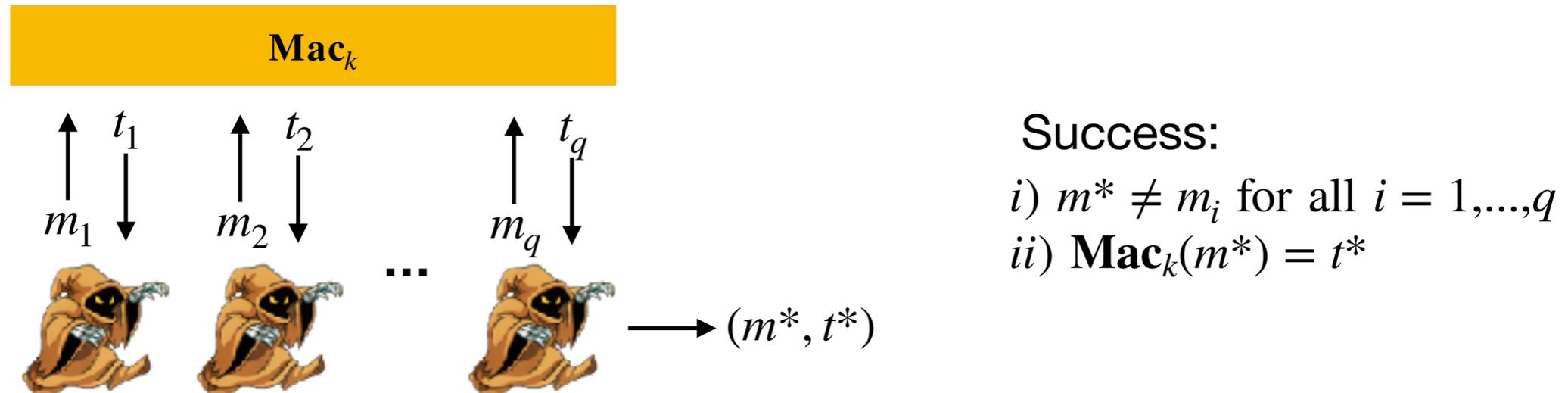
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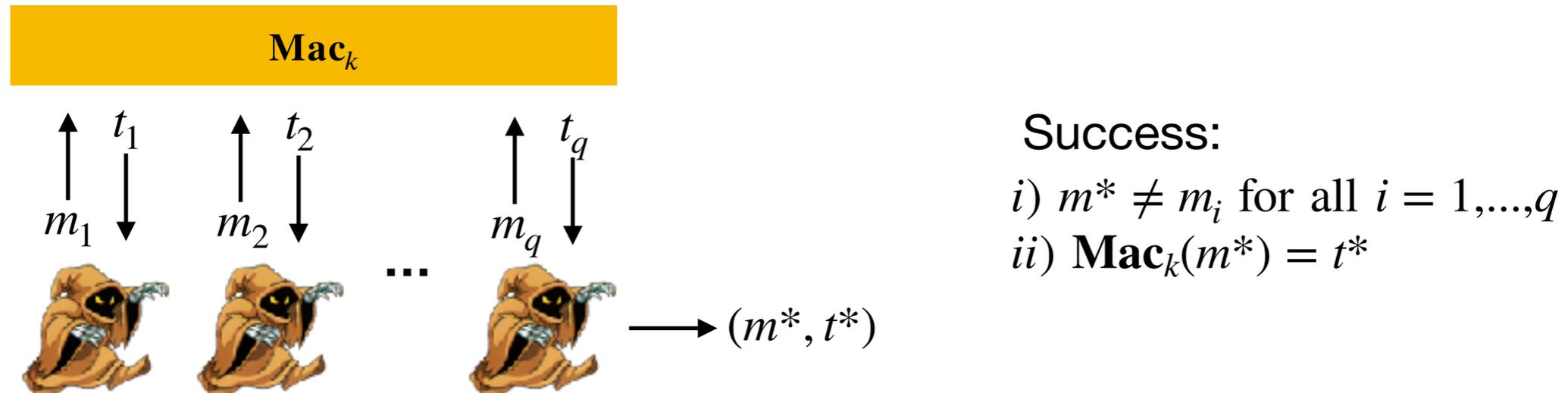


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Example:

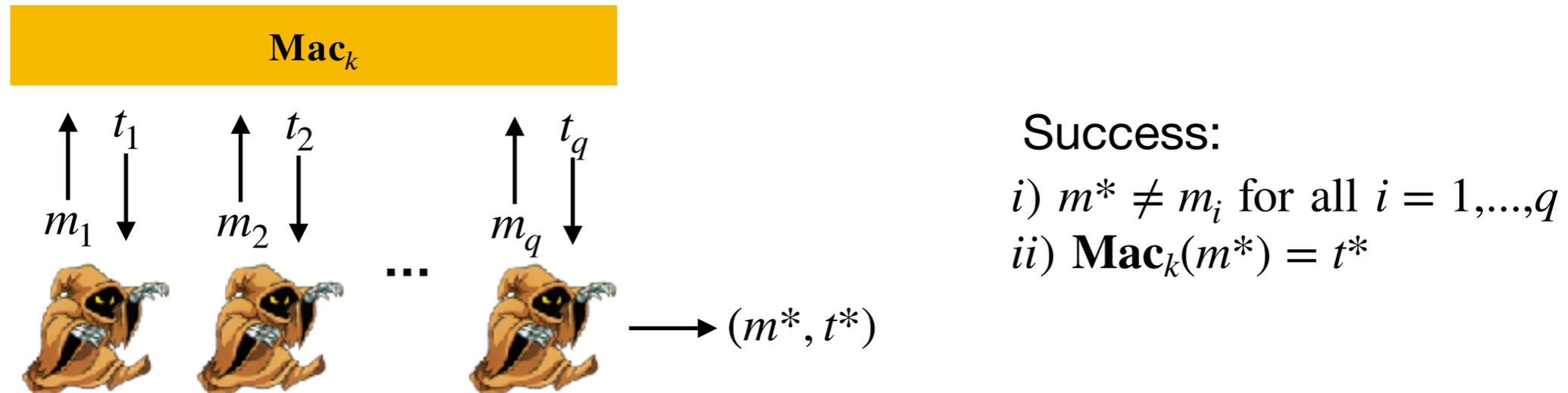
i) Query $m_1 = \sum_{m \in \{0,1\}^n} |m\rangle |0\rangle$ to obtain $\sum_{m \in \{0,1\}^n} |m\rangle |\mathbf{Mac}_k(m)\rangle$

ii) Measure in the computational basis to obtain $(m, \mathbf{Mac}_k(m))$ for random m

iii) Output $(m, \mathbf{Mac}_k(m))$

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EUFCMA doesn't make sense anymore...

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What does it mean for a function to be unpredictable against quantum?

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A good predictor:

key k specifies a random periodic function f_k with period p_k

$\mathbf{Mac}_k(p_k) = 0$, and $\mathbf{Mac}_k(x) = f_k(x) \forall x \neq p_k$

i) run period finding to find p_k

ii) output $(p_k, 0)$

Boneh Zhandry unforgeability

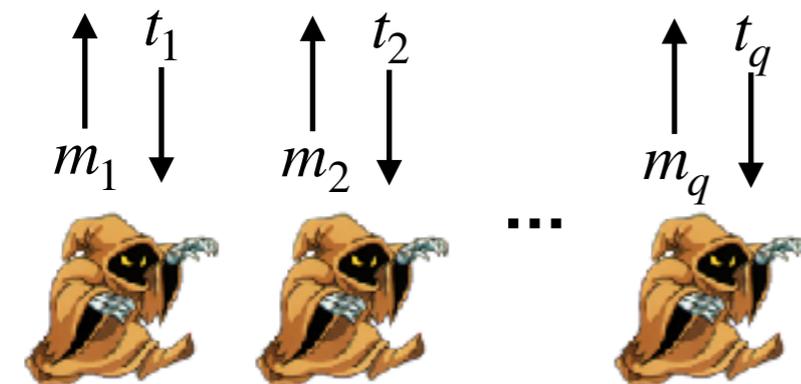
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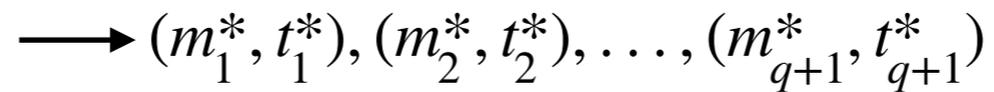
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$$\text{Mac}_k(m_i^*) = t_i^* \quad \forall i = 1, \dots, q + 1$$

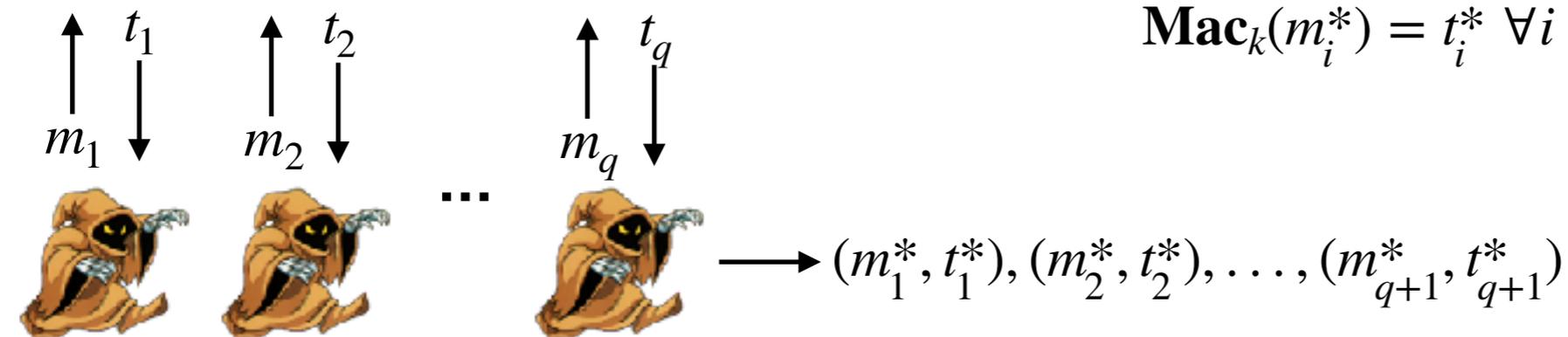


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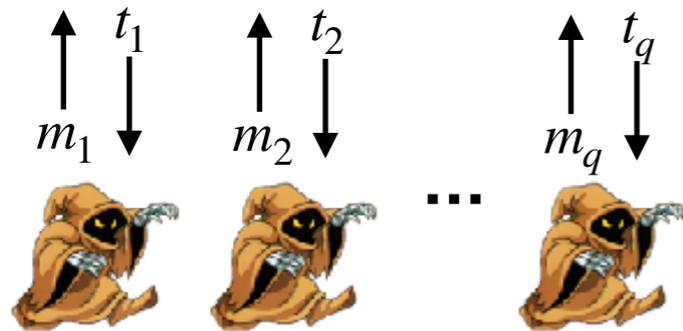
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Has some nice properties:

- Equivalent to **EUFCMA** for classical oracle
- A random function is BZ-unforgeable (BZ '13)

The right definition?

Mac_k

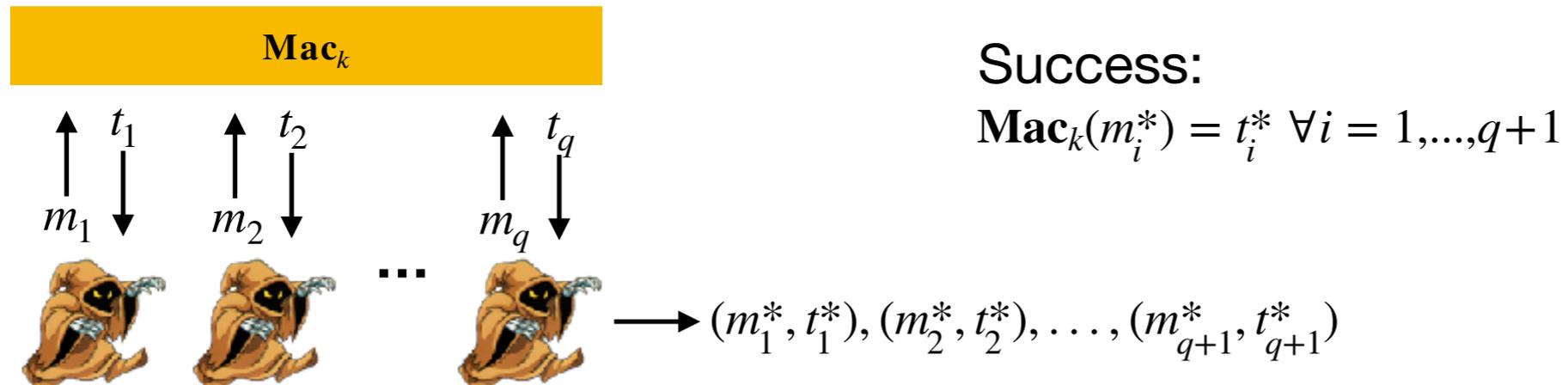


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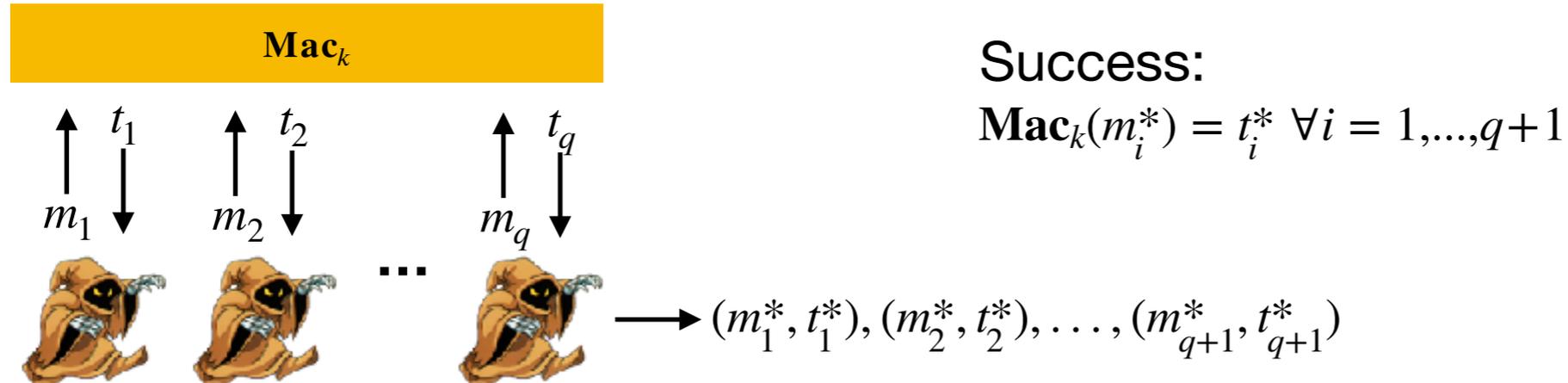


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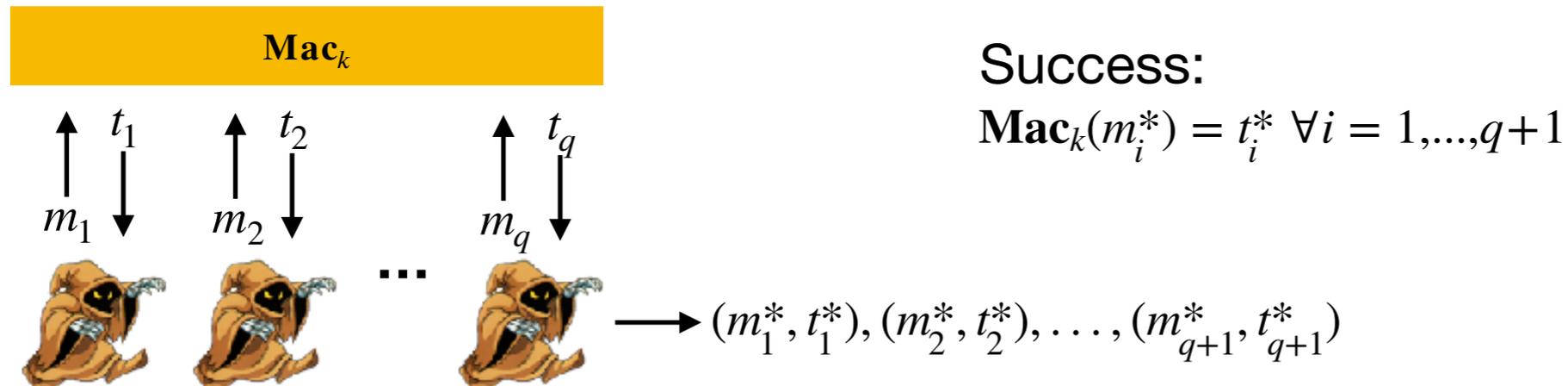
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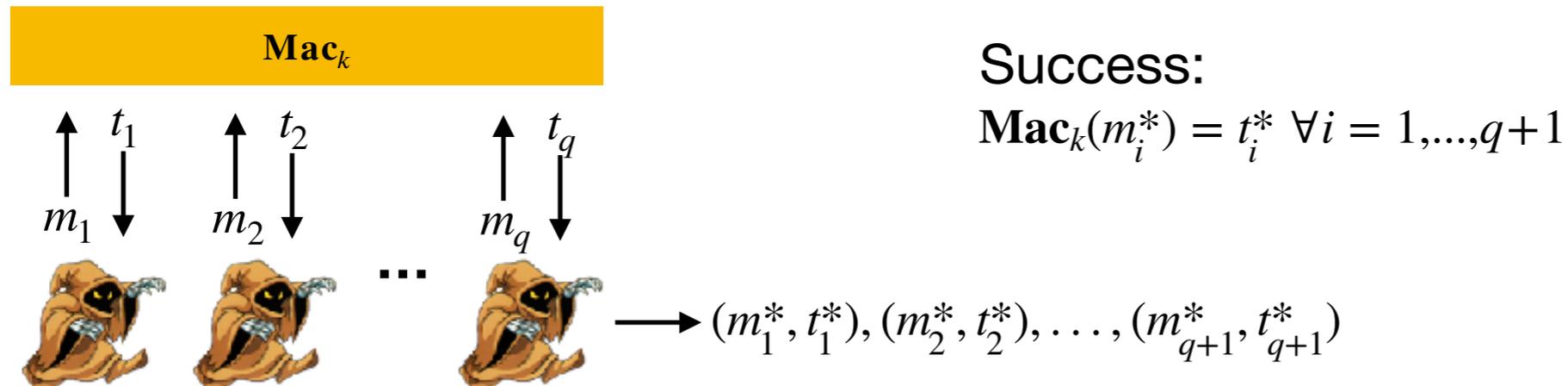
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Is our intuition right? One obstacle: “property finding” cannot be used.

Not the right definition!

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- Let f_0, f_1 be random functions; let A be a large random subgroup of \mathbb{Z}_2^n ;
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- MAC: $\mathbf{Mac}_k(bx) = f_b^A(x)$ with $k = (f_0, f_1, A)$.

random Simon problem
(but with large subgroup)

$b = 0$

a function which is only
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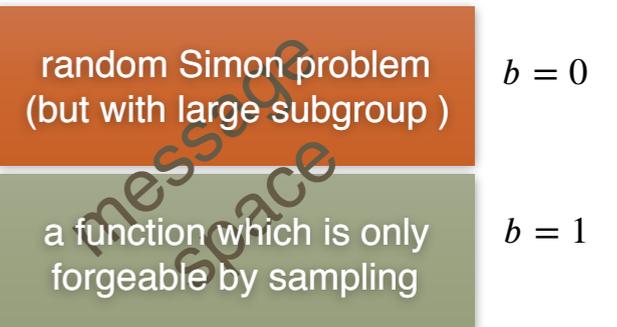
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Theorem (AMRS17). There are no efficient quantum algorithms which query \mathbf{Mac}_k once but output two distinct input-output pairs of \mathbf{Mac}_k .

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A MAC \mathbf{Mac}_k is blind-unforgeable if for every adversary \mathcal{A} with a quantum oracle for $B_\epsilon \mathbf{Mac}_k$

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Check, e.g., for random functions:

- if oracle is blinded...
- ... $\mathbf{Mac}_k(m)$ for blinded m is *independent* of post-query state,
- this adversary fails.



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- *oracle is blinded only on few random inputs...*

One-query attack: Fourier sample orange part,
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Blind Unforgeability



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Does this work?

- equivalent to **EUFCMA** in classical setting;
- random functions satisfy it;
- classifies the examples we have seen thus far correctly.

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random Simon problem
(but with large subgroup) f_0^A

a function which is only
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- so this adversary succeeds!

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Outlook

What's next?

- did we solve the problem?
- is blind-unforgeability the “right” notion of unforgeability against quantum adversaries?
- maybe: it does the right thing on all the examples we could think of;
- maybe not: it seems hard to prove that it implies **BZ** (does that matter?); we can come up with lots of seemingly inequivalent variants of **BU**.

In general: we need to develop and refine new techniques for quantum query complexity to suit “crypto needs”, e.g. to analyze

1. algorithms which only succeed on a small space of inputs;
2. algorithms which succeed with vanishing (but non-negligible) probability;
3. non-asymptotics: problems with an “easy/impossible” thresholds of one (or few) queries.